

Programming Languages:

Lecture 3

Chapter 3: Syntax and Semantics

Jinwoo Kim

jwkim@jjay.cuny.edu

- Introduction
- The General Problem of Describing Syntax
- Formal Methods of Describing Syntax
- Attribute Grammars
- Describing the Meanings of Programs: Dynamic Semantics

- **Syntax:** the form or structure of the expressions, statements, and program units
- **Semantics:** the meaning of the expressions, statements, and program units
- Syntax and semantics provide a language's definition
 - Users of a language definition
 - Other language designers
 - Implementers
 - Programmers (the users of the language)

- A *sentence* is a string of characters over some alphabet
- A *language* is a set of sentences
- A *lexeme* is the lowest level syntactic unit of a language (e.g., *, sum, begin)
- A *token* is a category of lexemes (e.g., identifier)

(Example)

```
index = 2 * count + 17;
```

| <i>Lexemes</i> | <i>Tokens</i> |
|----------------|---------------|
| Index | identifier |
| = | equal_sign |
| 2 | int_literal |
| * | mult_op |
| count | identifier |
| + | plus_op |
| 17 | int_literal |
| ; | semicolon |

Formal Definition of Languages

- Recognizers
 - A recognition device reads input strings of the language and decides whether the input strings belong to the language
 - Example: syntax analysis part of a compiler
 - Detailed discussion in Chapter 4
- Generators
 - A device that generates sentences of a language
 - One can determine if the syntax of a particular sentence is correct by comparing it to the structure of the generator

Formal Methods of Describing Syntax

- Backus-Naur Form and Context-Free Grammars
 - Most widely known method for describing programming language syntax
- Extended BNF
 - Improves readability and writability of BNF
- Grammars and Recognizers

- Context-Free Grammars
 - Developed by Noam Chomsky in the mid-1950s
 - Language generators, meant to describe the syntax of natural languages
 - Define a class of languages called context-free languages

Backus-Naur Form (BNF)

- Backus-Naur Form (1959)
 - Invented by John Backus to describe Algol 58
 - BNF is equivalent to context-free grammars
 - BNF is a *metalanguage* used to describe another language
 - In BNF, abstractions are used to represent classes of syntactic structures--they act like syntactic variables (also called *nonterminal symbols*)

- Non-terminals: BNF abstractions
- Terminals: lexemes and tokens
- Grammar: a collection of rules
 - Examples of BNF rules:
`<ident_list> → identifier | identifier, <ident_list>`
`<if_stmt> → if <logic_expr> then <stmt>`

BNF Rules

- A rule has a left-hand side (LHS) and a right-hand side (RHS), and consists of *terminal* and *nonterminal* symbols
- A grammar is a finite nonempty set of rules
- An abstraction (or nonterminal symbol) can have more than one RHS

```
<stmt> → <single_stmt>  
        | begin <stmt_list> end
```

Describing Lists

- Syntactic lists are described using recursion

```
<ident_list> → ident  
              | ident, <ident_list>
```

- A derivation is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

An Example Grammar

`<program> → <stmts>`

`<stmts> → <stmt> | <stmt> ; <stmts>`

`<stmt> → <var> = <expr>`

`<var> → a | b | c | d`

`<expr> → <term> + <term> | <term> - <term>`

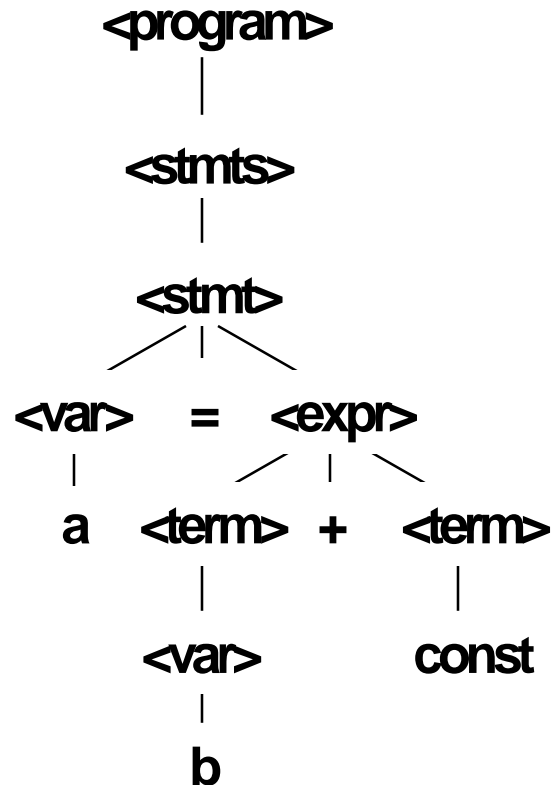
`<term> → <var> | const`

An Example Derivation

`<program> => <stmts>`
`=> <stmt>`
`=> <var> = <expr>`
`=> a = <expr>`
`=> a = <term> + <term>`
`=> a = <var> + <term>`
`=> a = b + <term>`
`=> a = b + const`

- Every string of symbols in the derivation is a sentential form
- A sentence is a sentential form that has only terminal symbols
- A leftmost derivation is one in which the leftmost nonterminal in each sentential form is the one that is expanded
- A derivation may be neither leftmost nor rightmost

- A hierarchical representation of a derivation



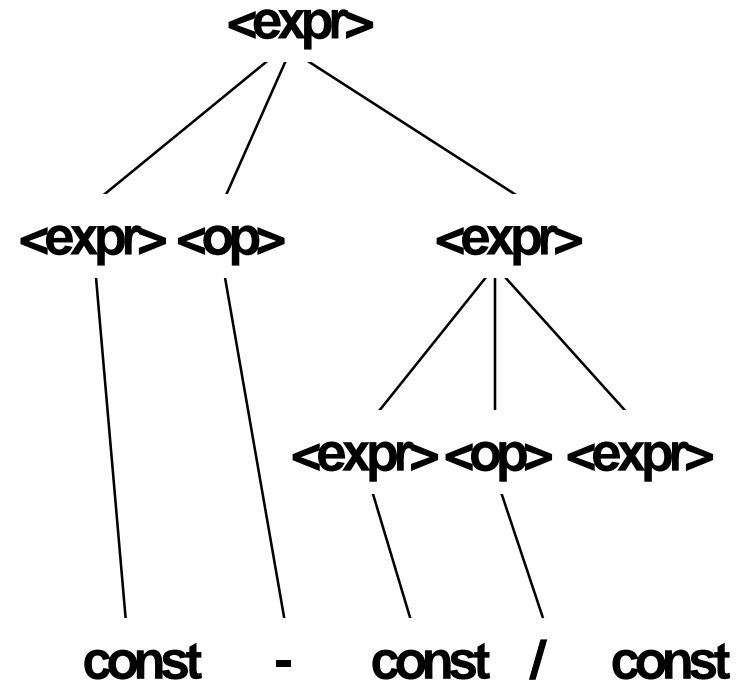
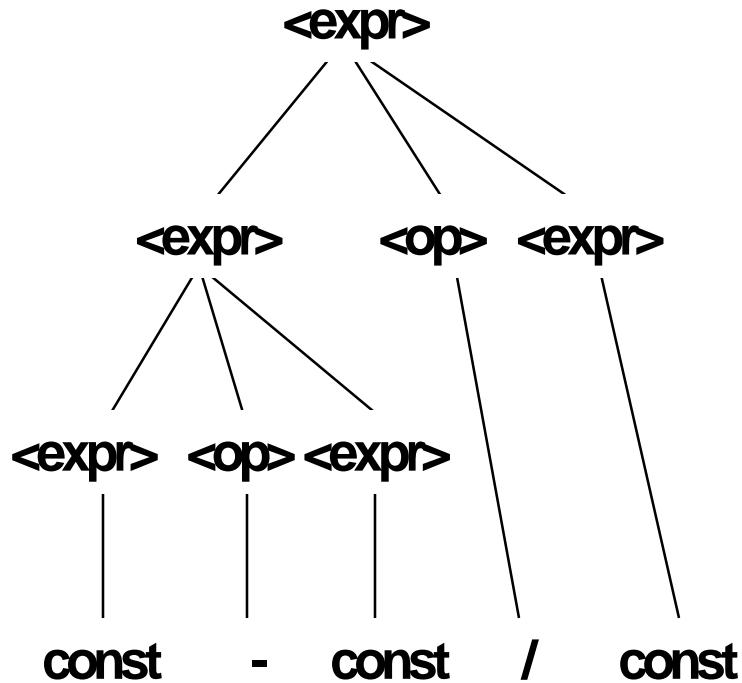
Ambiguity in Grammars

- A grammar is *ambiguous* if and only if it generates a sentential form that has two or more distinct parse trees

An Ambiguous Expression Grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

$\langle \text{op} \rangle \rightarrow / \mid -$

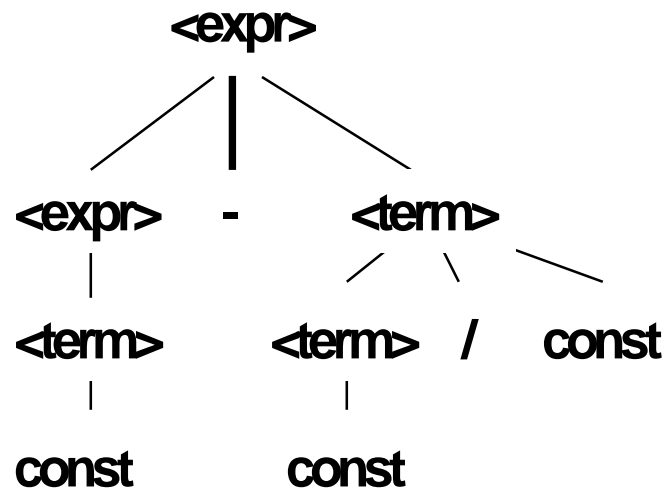


An Unambiguous Expression Grammar

- If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

`<expr> → <expr> - <term> | <term>`

`<term> → <term> / const | const`

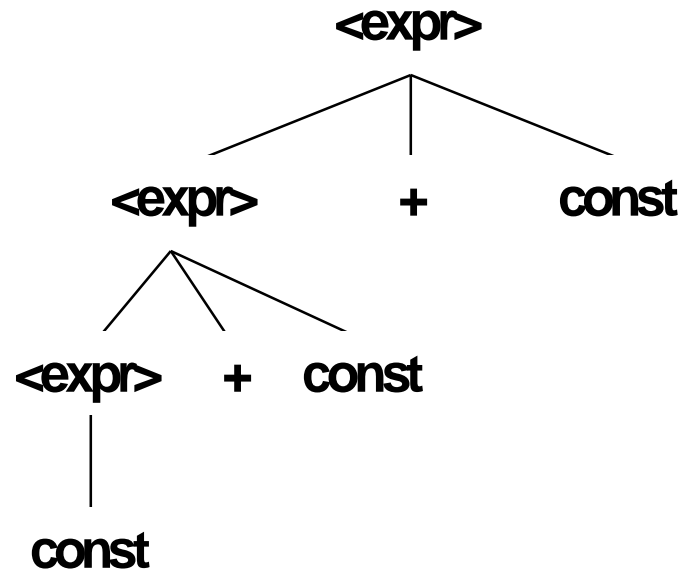


Associativity of Operators

- Operator associativity can also be indicated by a grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \text{const}$ (ambiguous)

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \text{const} \mid \text{const}$ (unambiguous)



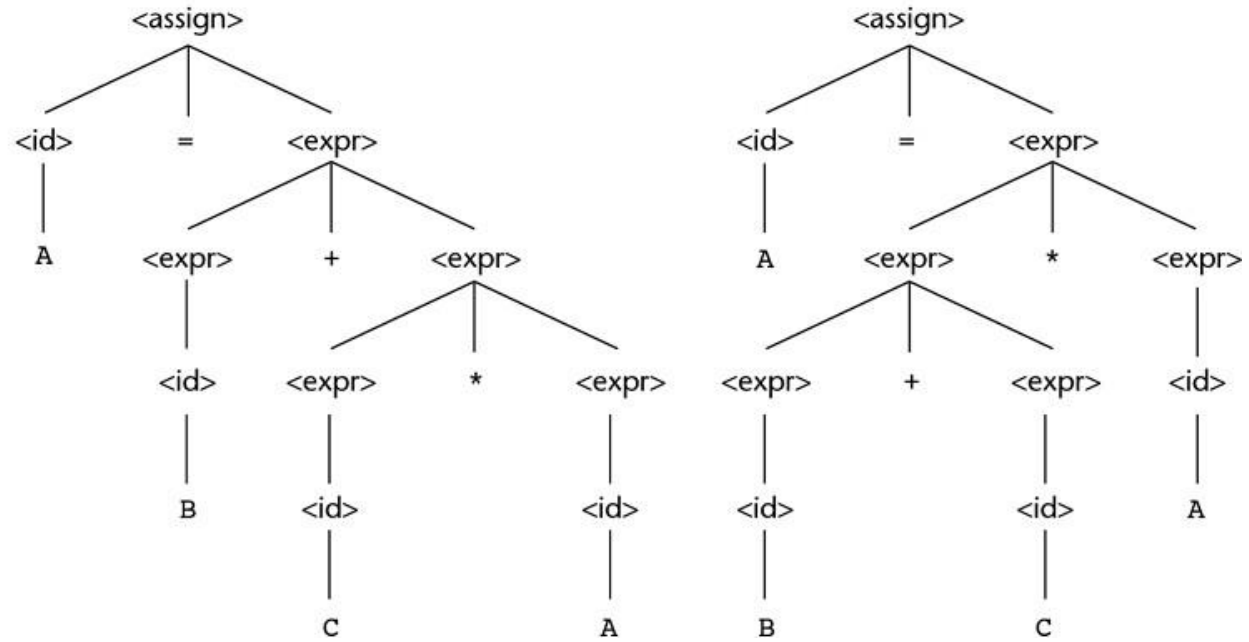
EXAMPLE 3.3

An Ambiguous Grammar for Simple Assignment Statements

$$\begin{aligned}\langle \text{assign} \rangle &\rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle \\ \langle \text{id} \rangle &\rightarrow A \mid B \mid C \\ \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle \\ &\quad \mid \langle \text{expr} \rangle * \langle \text{expr} \rangle \\ &\quad \mid (\langle \text{expr} \rangle) \\ &\quad \mid \langle \text{id} \rangle\end{aligned}$$

Figure 3.2

Two distinct parse trees for the same sentence,
A = B + C * A



EXAMPLE 3.4**An Unambiguous Grammar for Expressions**
$$\begin{aligned} \langle \text{assign} \rangle &\rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle \\ \langle \text{id} \rangle &\rightarrow A \mid B \mid C \\ \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &\quad \mid \langle \text{term} \rangle \\ \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &\quad \mid \langle \text{factor} \rangle \\ \langle \text{factor} \rangle &\rightarrow (\langle \text{expr} \rangle) \\ &\quad \mid \langle \text{id} \rangle \end{aligned}$$

Figure 3.3

The unique parse tree for $A = B + C * A$ using an unambiguous grammar

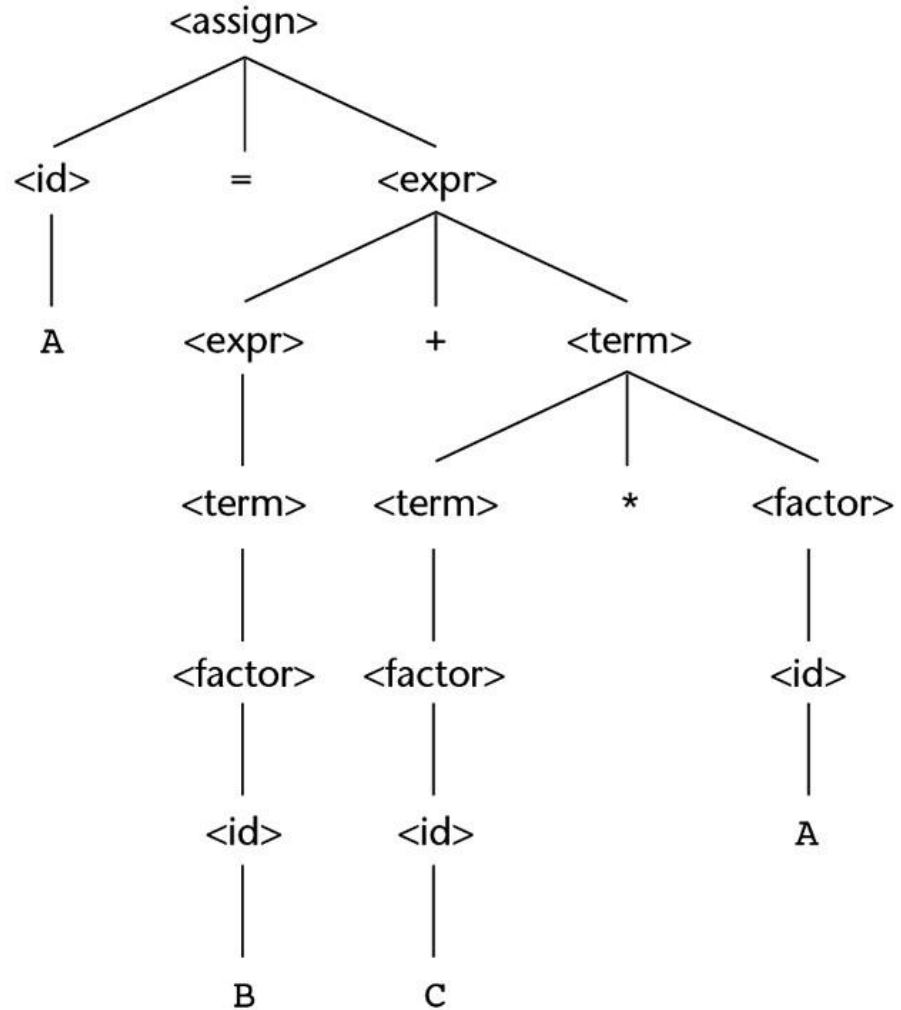
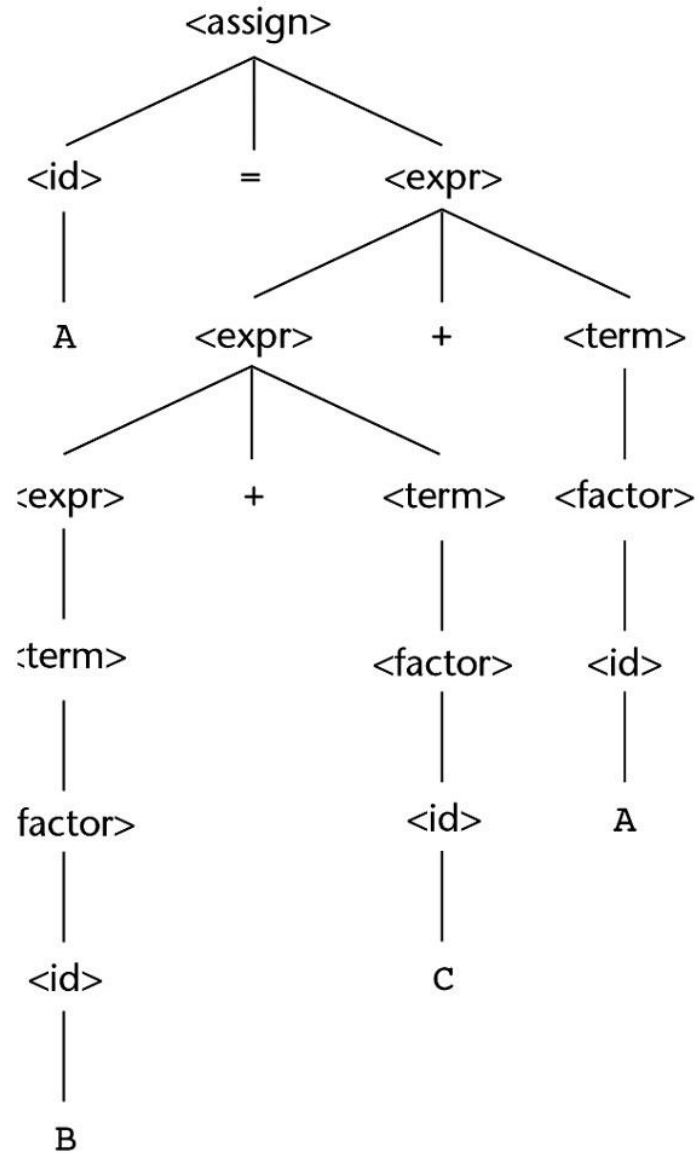


Figure 3.4

A parse tree for $A = B + C + A$ illustrating the associativity of addition



Extended BNF

- Optional parts are placed in brackets []
`<proc_call> -> ident [(<expr_list>)]`
- Alternative parts of RHSs are placed inside parentheses and separated via vertical bars
`<term> -> <term> (+|-) const`
- Repetitions (0 or more) are placed inside braces { }
`<ident> -> letter {letter|digit}`

- **BNF**

$$\begin{aligned} \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &\quad | \langle \text{expr} \rangle - \langle \text{term} \rangle \\ &\quad | \langle \text{term} \rangle \end{aligned}$$
$$\begin{aligned} \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &\quad | \langle \text{term} \rangle / \langle \text{factor} \rangle \\ &\quad | \langle \text{factor} \rangle \end{aligned}$$

- **EBNF**

$$\begin{aligned} \langle \text{expr} \rangle &\rightarrow \langle \text{term} \rangle \{ (+ \mid -) \langle \text{term} \rangle \} \\ \langle \text{term} \rangle &\rightarrow \langle \text{factor} \rangle \{ (* \mid /) \langle \text{factor} \rangle \} \end{aligned}$$

EXAMPLE 3.5

BNF and EBNF Versions of an Expression Grammar

BNF:

$$\begin{aligned} \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &\quad | \langle \text{expr} \rangle - \langle \text{term} \rangle \\ &\quad | \langle \text{term} \rangle \\ \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &\quad | \langle \text{term} \rangle / \langle \text{factor} \rangle \\ &\quad | \langle \text{factor} \rangle \\ \langle \text{factor} \rangle &\rightarrow \langle \text{exp} \rangle ** \langle \text{factor} \rangle \\ &\quad | \langle \text{exp} \rangle \\ \langle \text{exp} \rangle &\rightarrow (\langle \text{expr} \rangle) \\ &\quad | \text{id} \end{aligned}$$

EBNF:

$$\begin{aligned} \langle \text{expr} \rangle &\rightarrow \langle \text{term} \rangle \{ (+ | -) \langle \text{term} \rangle \} \\ \langle \text{term} \rangle &\rightarrow \langle \text{factor} \rangle \{ (* | /) \langle \text{factor} \rangle \} \\ \langle \text{factor} \rangle &\rightarrow \langle \text{exp} \rangle \{ ** \langle \text{exp} \rangle \} \\ \langle \text{exp} \rangle &\rightarrow (\langle \text{expr} \rangle) \\ &\quad | \text{id} \end{aligned}$$

- BNF and context-free grammars are equivalent meta-languages
 - Well-suited for describing the syntax of programming languages
- An attribute grammar is a descriptive formalism that can describe both the syntax and the semantics of a language
- Three primary methods of semantics description
 - Operation, axiomatic, denotational

Homework #2

- Read articles introduced in this lecture
 - The Chomsky Hierarchy
 - http://jjcweb.jjay.cuny.edu/~jwkim/class/csci374-fall-24/Chomsky_Hierarchy.pdf
- Problem Solving (Chapter 3)
 - 2.c, 3, 6.a, 8, 9, 10, 11, 15, 16, 17
 - HW 2
 - Refer class homepage for Chapter 3 problems
 - Please email your hw in word or pdf format
 - No late homework will be accepted